The University of Tokyo, Komaba
PEAK Programs in English at Komaba

## Expected background knowledge in Mathematics for students on the PEAK Environmental Sciences course

| $\boldsymbol{x}$ - no coverage | L - very limited coverage | P - partial coverage | $\boldsymbol{V}$ - covered |
| :--- | :--- | :--- | :--- |


| Subject | Coverage in common school examination systems |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | GCSE | IB Standard | SAT | A-level | IB Higher | AP Calculus |
| 1. Equations and inequalities |  |  |  |  |  |  |
| a) Numbers and expressions <br> Real numbers <br> Expansion and factorization of a polynomial | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| b) Linear inequalities | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| c) Quadratic equations | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| 2. Quadratic functions |  |  |  |  |  |  |
| a) Quadratic functions and their graphs | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| b) Variation in values of quadratic functions <br> Maximum value and minimum value of a quadratic function Quadratic inequalities | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| 3. Figures and measurements |  |  |  |  |  |  |
| a) Trigonometric ratios <br> Sine, cosine, tangent <br> Relations between trigonometric ratios | P | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| b) Trigonometric ratios and figures Sine formulas, cosine formulas Measurement of figures | P | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| 4. Plane figures |  |  |  |  |  |  |
| Properties of triangles Properties of circles | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| 5. Set theory and logic |  |  |  |  |  |  |
| Sets and the number of elements Propositions and proofs | X | P | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| 6. The number of possible outcomes and probability |  |  |  |  |  |  |
| Permutations, Combinations Probability and its fundamental laws Independent trials and probability | P | X | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| 7. Expressions and proofs / equations of higher degree |  |  |  |  |  |  |
| a) Expressions and proofs Division of polynomials, fractional expressions Proofs of equalities and inequalities | X | $\checkmark$ | P | $\checkmark$ | $\checkmark$ | - |
| b) Equations of higher degree Complex numbers and quadratic equations Equations of higher degree | X | X | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| 8. Figures and equations |  |  |  |  |  |  |
| a) Points and lines Coordinates of a point Equation of a line | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| b) Circles <br> Equation of a circle <br> Relative position of a circle and a line | $\checkmark$ | P | $\checkmark$ | $\checkmark$ | P | - |
| 9. Various functions |  |  |  |  |  |  |
| a) Trigonometric functions General angles <br> Trigonometric functions and their basic properties Addition theorems for trigonometric functions | L | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| b) Exponential and logarithmic functions <br> Expansion of exponents <br> Exponential functions <br> Logarithmic functions | X | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |


| Subject | Coverage in common school examination systems |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | GCSE | IB Standard | SAT | A-level | IB Higher | Calculus |
| 10. The concept of differentiation / integration |  |  |  |  |  |  |
| a) The concept of differentiation <br> Differential coefficients and derivatives <br> Applications of the derivative <br> Tangent lines, increase/decrease in function value | X | X | X | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| b) The concept of integration Indefinite integrals and definite integrals Areas of figures | X | X | X | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| 11. Sequences (Progressions) of numbers |  |  |  |  |  |  |
| a) Sequences and their sums <br> Arithmetic sequences (Arithmetical progressions) and geometric <br> sequences (geometrical progressions) <br> Various sequences | X | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |
| b) Recurrence formulae and mathematical induction Recurrence formulae and sequences Mathematical induction | x | P | P | $\checkmark$ | $\checkmark$ | - |
| 12. Vectors |  |  |  |  |  |  |
| Vectors in a plane <br> Vectors and their operations <br> Scalar product (Inner product) of vectors | P | $\checkmark$ | P | $\checkmark$ | $\checkmark$ | - |
| 13. Limits |  |  |  |  |  |  |
| Limits of sequences <br> Limit of $\{r n\}$ <br> Sum of an infinite geometric series | X | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | - |


| $\boldsymbol{X}$ - no coverage | L - very limited coverage | $P$ - partial coverage | $\boldsymbol{V}$ - covered |
| :--- | :--- | :--- | :--- |

